Research Report

Writing Fault-Tolerant Applications Using Resilient X10

Kiyokuni Kawachiya

IBM Research - Tokyo
IBM Japan, Ltd.
NBF Toyosu Canal Front Building
6-52, Toyosu 5-chome, Koto-ku
Tokyo 135-8511, Japan

Limited Distribution Notice
This report has been submitted for publication outside of IBM and will be probably copyrighted if accepted. It has been issued as a Research Report for early dissemination of its contents. In view of the expected transfer of copyright to an outside publisher, its distribution outside IBM prior to publication should be limited to peer communications and specific requests. After outside publication, requests should be filled only by reprints or copies of the article legally obtained (for example, by payment of royalties).
Abstract

X10 is a programming language that internally supports distributed computing. X10 applications can run over multiple "places" (computing nodes), and perform distributed computing by changing the execution place using "at" statements. However, in a conventional X10 environment, when a node that handles a place fails, the entire processing of that X10 application is aborted. To address this problem, we have been extending X10 to "Resilient X10", where a node failure is reported as a DeadPlaceException and the execution can continue using the remaining nodes. In this paper, we explain how to construct fault-tolerant distributed applications using Resilient X10 functions. Three basic methods are introduced to handle the node failures: (a) Ignore failures and use the results from the remaining nodes, (b) Reassign the failed node’s work to the remaining nodes, or (c) Restore the computation from a periodic snapshot. We also describe a fault-tolerant extension of the existing distributed X10 library DistArray. These modifications to add fault tolerance were very small, and the modified code can still run on standard X10 as long as node failure does not occur. The impacts on execution performance caused by the modifications are also evaluated.

Keywords Resilient X10, Fault tolerance, Distributed programming

1. Introduction

X10 [22] is a programming language that supports distributed computing. However in the original X10 implementation, when a computing node crashes, the whole X10 application is aborted even if the other nodes are alive. To address this problem, we are developing an extended version called “Resilient X10” [3], where the node failure is reported as an exception and the execution can continue using the remaining nodes. This paper explains how fault-tolerant distributed applications can be constructed using Resilient X10 functions.

For the execution model on a distributed environment, X10 uses PGAS (Partitioned Global Address Space) [13]. As the name indicates, the PGAS model provides a global address space, but it is partitioned into multiple places, each of which basically corresponds to a computing node. Data can be referenced from any place, but an activity must move to the place using an “at” statement to access the data.

A node failure can be considered as the death of a place in X10, which means that data on the place become inaccessible. However, since the address space is explicitly partitioned, it is relatively easy in the PGAS model to continue the execution by detaching the failed node (place). For example, when the target place of an at statement dies, the processing can continue if the caller receives some kind of notification. In the Resilient X10 we are developing, a newly defined exception, DeadPlaceException, is raised for this situation.

Unfortunately, simple notification of the place death is not sufficient to continue the application. To achieve fault tolerance, the application (or libraries) must reconfigure the processing appropriately based on the notification. In this paper, we introduce the following three basic methods to handle the notification: (a) Ignore failures and use the results from the remaining nodes, (b) Reassign the failed node’s work to the remaining nodes, or (c) Restore the computation from a periodic snapshot. Programming examples for these three methods in Resilient X10 are provided. We also show a fault-tolerant extension of the existing distributed X10 library DistArray. These modifications to add fault tolerance are very small, and the modified code can still run on standard X10 as long as node failure does not occur. The major contributions of this paper are:

- An analysis of multiple approaches to add fault tolerance to existing distributed applications, proving that they can be implemented with minimal modifications using Resilient X10.
- An evaluation of the developed fault-tolerant applications from various perspectives in a real distributed environment.
2. Fault Tolerance Support in Resilient X10

For programming parallel and distributed applications, it is very important how the parallelism and distributed memory structure are exposed to the programmer. The upper figures in Figure 1 show three variations. A “shared memory” model such as OpenMP [12], where the parallelization is managed implicitly, makes the programming easier, but fine-grain tuning to maximize the use of hardware may be difficult. In contrast, a “message passing” model such as MPI [9], where all of the communications are explicitly described, always requires the programmer to be fully aware of the underlying hardware configuration.

The PGAS used by X10 can be regarded as being between these two approaches, with a global address space that is partitioned into multiple “places”. The place is an abstraction of memory locality and typically corresponds to a computing node. Each unit of data belongs to a specific place and can be accessed only in that place, but it can be referenced (pointed to) from any place. By providing such an abstracted view of the underlying parallel/distributed environment instead of concealing it, X10 tries to offer high productivity for high performance computing. The PGAS model is also used in other languages such as UPC (Unified Parallel C) [18] and CAF (Co-Array Fortran) [20]. Since X10 supports the arbitrary creation of asynchronous activities, its execution model is sometimes called APGAS (Asynchronous PGAS).

2.1 APGAS Execution Model

The lower part of Figure 1 shows X10’s APGAS execution model. A global address space is partitioned into multiple places, which can hold multiple activities and objects.

An activity is a kind of lightweight thread sequentially executed in a place. It is created by an async statement and can move to another place using an at statement, through which parallel and distributed processing is made possible. A finish statement is used to wait for the termination of activities (including grandchildren) created inside that block. At this time, exceptions are propagated by being encapsulated in a MultiExceptions object. By using this “Rooted Exception Model”, X10 programs can handle exceptions thrown by asynchronous activities.

An object is a mutable data structure that belongs to a specific place and can only be accessed by the activities running in that place. However, objects can be globally (remotely) referenced by using GlobalRef [6, 15]. The global reference contains information about where the object exists, so activities can move to that place to access the object. For example, a statement “data = at (pref) pref();” indicates to move to the place of the global reference pref and read its value. X10 also provides a distributed array structure named DistArray whose elements are scattered over multiple places. Each element can be manipulated by activities in the same place.

Figure 2 shows a Hello World program written in X10 and an execution example using four places. A new asynchronous activity is created in each of the places by the at and async statements in Line 4, and a message “Hello from Place(n)” is printed in a parallel and distributed manner. The termination of the activities are waited for by the finish statement ending at Line 7, and the program terminates its execution.

2.2 Resilient X10

Distributed processing with X10 can be done by running each place as a process on a different computing node. When a node is broken, all of the activities and data in that place are lost, and the entire X10 processing is aborted in standard X10. However, since the address space partitioning is visible from applications, localizing the impact of place death is relatively easy in the PGAS model. Consider the case when Place 1 in the lower part of Figure 1 dies. Three activities, two objects,
and some parts of two distributed arrays in that place are lost, but the remaining portions in other places are not affected. Global references to the dead place became inaccessible, but can remain in live places. By exploiting this, we have been extending X10 to continue the execution using the remaining nodes (places), in our new language “Resilient X10” [3].

In Resilient X10, the newly defined exception DeadPlaceException (shortened to DPE in the following explanation) is thrown for a place death. Concretely, if an activity is being moved (or trying to move) to a dead place, the corresponding statement at an assertion throws the DPE. When an activity is asynchronously executing in a dead place using the async statement, the finish statement governing the activity will throw a MultipleExceptions object which contains the DPE (and possibly other exceptions in the block). The id of the dead place can be checked through the place field of the DPE. Some utility methods are also provided, such as Place.isDead to check if a specified place is dead or not, and Place.numDead to check the number of dead places.

These functions make it possible to write fault-tolerant X10 applications that can continue to run on the remaining nodes even when some places are lost due to node failures. Figure 3 shows a simple example. This program performs do_something in all of the places, and simply prints “Place(n) died” for the DPE notification (Lines 6–7).

To process a finish statement appropriately even when some activities have been lost due to node failure, the execution status of the activities (the number of activities running on each place) governed by the finish must be recorded securely and not lost by the failure. Resilient X10 stores such kinds of critical information in a reliable storage area named Resilient Storage. We have implemented several variations of the Resilient Storage, and the most stable version in our current implementation is the one which uses Place 0 (the place where main is executed) for this purpose.

The Resilient X10 function is included as a technology preview in X10 2.4.1 (released in December 2013) and later versions, and can be enabled by specifying an environment “X10_RESILIENT_MODE=1”. Resilient X10 can run with either of two X10 implementations: Native X10, compiled to C++ and executed natively, and Managed X10 [6, 17], compiled to Java™ and executed on multiple Java VMs. The communication layer is limited to sockets, and MPI [9] and PAMI [7] are not yet supported. Refer to [3] for more implementation details, and [2] for the semantics of the place-death handling.

3. Fault-Tolerant X10 Applications

Currently, Resilient X10 provides only a few programming interfaces: DeadPlaceException to notify the application of place death and support methods such as Place.isDead and Place.numDead, but these are sufficient to add fault tolerance to existing distributed X10 applications.

However for this to work, it is necessary to understand how the application is doing the distributed processing and how the execution can be continued after a node failure. Depending on these situations, the approach to adding the fault tolerance will differ. This section explains two methods to handle node failures:

(a) Ignore the failures and use the results from the remaining nodes, or
(b) Reassign the failed node’s work to the remaining nodes.

A third method will be added in Section 4.

3.1 MontePi

Figure 4 is an example of adding fault tolerance to an application which approximates π by using a Monte Carlo method. The core part of the computation is the for loop at Lines 12–15, which repeatedly checks if randomly generated coordinates (x, y) are inside a circle of radius 1.0. After ITERS number of trials, the result is added to a global result data pair stored at Place 0 (Lines 17–20). This series of processes is performed in parallel at each place, and when all of them finish, the value of π is finally calculated from the result (Lines 26–27).

If a node fails during the computation, the place executing on that node dies and the at statement at Line 9 throws a DeadPlaceException. This exception is caught by the catch statement at Line 22 and just ignored. In the now dead place, the at statement at Line 17 is never executed, so the global result is not updated. Therefore, only the results from living nodes will be used for the final calculation. The result may become less accurate because the number of trials of the

---

1 This version has a limitation that X10 execution is aborted if Place 0 is dead. The fault-tolerant applications shown in this paper also use the assumption that Place 0 never dies.
Monte Carlo method is reduced, but it is not completely broken by the node failure. This program also prints the total number of trials as reference information.

In this example, the code that was added for fault tolerance is only the try statement at Line 8 and the catch statement spanning Lines 22–24.

3.2 KMeans

KMeans is a basic algorithm for clustering analysis, categorizing n points in d-dimensional space into K clusters. The basic operation is an iteration of: (1) Categorizing the n points based on the coordinates of the K clusters, and (2) Making the centroid of the points to the new coordinates of each cluster. The iteration ends when the differences in the coordinates between iterations becomes smaller than a threshold. In a distributed environment, Step (1) can be done in parallel by assigning n points to each computing node and returning the results necessary for Step (2). Since the coordinates of the n points do not change, they can be copied in advance.

For such programs, fault tolerance can be supported by reassigning the work only to available nodes. Figure 5 shows the skeleton of a fault-tolerant KMeans application based on this approach. In this figure, "/* ... */" explains the processing of the omitted part. The complete code is listed in Figures 9 and 10 of appendix. The work reassignment is performed by the code in Lines 9–17. The number of available places is determined in Line 9, and the number of points to be processed at each place is calculated in Lines 10–11. Lines 14–17 process the computation at the live places in parallel by skipping the dead places (Line 15).

When a place dies during the execution, a DeadPlaceException (enclosed by a MultipleExceptions) is thrown for the finish statement in Line 14, and caught by the catch statement in Line 23. The notification is simply ignored in this program, and retry of the lost computation or disposal of other results are not performed. This is because even the partial results can still make the convergence faster for the KMeans computation (we call this approach decimation [3]). However, to make the final results precise, the convergence check is performed only when all of the points are processed.

In this example, the code added for fault tolerance is about 10 lines, including the parts omitted from Figure 5.

4. Fault-Tolerant X10 Libraries

The MontePi and KMeans examples in the previous section were written only using basic X10 constructs. However, for efficiently writing large distributed applications, library support is crucial. As one of these libraries, X10 supports distributed array (DistArray), where the elements are scattered over multiple places,
4.1 Resilient DistArray

A large-scale distributed application typically has an SPMD structure, where each computing node executes the same processing on a small part of the large amount of data. A DistArray is a data structure suitable for such processing. The elements of the array are divided into multiple places and processed by activities running on the owning places. How to distribute the elements among the places can be flexibly defined by using a Dist structure. See the X10 documents [15] for the details.

Upon a node failure, the DistArray elements belonging to the dead place become inaccessible, so the SPMD processing cannot continue. To resume the processing, the distributed array must be rearranged among the remaining places while restoring all of the element data. The ResilientDistArray is a fault-tolerant extension of the distributed array to support this function. The current version is implemented as an independent class which contains a DistArray field, requiring about 200 lines of code. We are considering integrating the function into the standard distributed array in the future.

5 Currently X10 has two implementations of distributed array [15]. The one in x10.regionarray package supports complex and flexible element distribution, and the other in x10.array package is simple, but faster. There is a fault-tolerant extension for both of them, but the explanation in this paper uses the x10.regionarray implementation.

4.2 HeatTransfer

As an example using the ResilientDistArray, we selected the “HeatTransfer” program in this section. This is an application to compute the heat diffusion through a two-dimensional grid represented by an array. Each element of the array holds the heat value of a grid point, and is repeatedly updated by the average of surrounding four points until convergence. This is a “stencil” computation pattern, which is very common in HPC applications. By using DistArray, HeatTransfer can be easily implemented as a distributed program using multiple computing nodes, and several variations are included as examples in the X10 distribution.

Figure 7 shows the skeleton of a fault-tolerant HeatTransfer application using ResilientDistArray. The complete code is listed in Figure 11 of appendix. The for loop of Lines 15–29 is repeated until the result converges. Inside the loop, for each element of the DistArray, a new heat value is calculated in parallel at each place (Lines 23–25). To support fault tolerance, a new snapshot of DistArray A is created at every 10th iteration (Line 27).

When a node failure occurs during the execution, a DeadPlaceException (enclosed by a MultipleExceptions) is caught by the catch statement in Line 28, and the processException method is called. This method removes the dead place from the LivePlaces list and sets the restore_needed flag (Line 36). If this flag is set at the beginning of an iteration (Line 17), then DistArray A is reconstructed over the remaining places using the livePlaces information, and the element values are restored from the latest snapshot (Lines 18–
class ResilientHeatTransfer {
  static val N = 28; // size of grid
  static val livePlaces = new ArrayList[Place]();
  static val restore_needed = new Cell[Boolean](false);

  public static def main(args:Rail[String]) {
    for (p1 in Place.places()) livePlaces.add(p1);
    // initialize Region and Dist
    val BigR = Region.make(0..(N+1), 0..(N+1)); // surroundings
    val BigD:Dist(2) = Dist.makeBlock(BigR, 0,
      new SparsePlaceGroup(livePlaces.toRail()));
    // create a DistArray, each element holds a heat value
    val A = ResilientDistArray.make[Double](BigR, ...);
    A.snapshot(); // create the initial snapshot
    for (iter in 1..ITERATIONS) { // iterate until convergence
      if (restore_needed()) { // if some places died
        BigD = Dist.makeBlock(BigR, 0); // recreate Dist, and
        A.restore(BigD); // restore elements from the snapshot
        restore_needed() = false;
      }
      // /* compute new heat values for A's local elements */
      /* if converged, exit the for loop */
      if (iter % 10 == 0) A.snapshot(); // create a snapshot
      catch (e:Exception) { processException(e:); }
    } // end of for (iter)
    /* print the result */
  }

  private static def processException(e:Exception) { // exception
    if (e instanceof DeadPlaceException) {
      val deadPlace = (e as DeadPlaceException).place;
      livePlaces.remove(deadPlace); restore_needed() = true;
    } else /* handle MultiPlaceExceptions recursively */
  }
}

Figure 7. Fault-tolerant HeatTransfer (skeleton).

20). The execution is slightly unwound by this, but can be resumed by detaching the failed node.

In this example, the modifications for fault tolerance other than replacing DistArray with ResilientDistArray involve about 25 lines, including the parts omitted from Figure 7. This may seem to be relatively large for such a small application, but we believe larger DistArray applications can be made fault tolerant using the same approach, and the modification ratio will be smaller for more typical applications. Since half of the modifications are in the exception-handling code of processException, it can also be considered to provide this method as a library.

5. Evaluation

This section shows various evaluations of fault tolerance support using the applications from previous sections: MontePi, KMeans, and HeatTransfer.

5.1 Modification Amount

As explained in each section, the modifications necessary to add fault tolerance were very small: only 4 lines for MontePi, about 10 lines for KMeans, and about 25 lines for HeatTransfer. Adding the snapshot and restore functions to DistArray was done in about 200 lines of code. Note that all of these fault-tolerant programs will still run on standard X10 as long as node failure does not occur.

As shown above, Resilient X10 makes it possible to add fault tolerance to existing distributed applications with very small modifications. However, the best approach to adding the fault tolerance depends on the structure of each application. Therefore, we discussed three typical methods in this paper: (a) Ignore failures and use the results from the remaining nodes (MontePi), (b) Reassign the failed node’s work to the remaining nodes (KMeans), or (c) Restore the computation from a periodic snapshot (HeatTransfer).

5.2 Execution Performance

Next, we evaluated the impact of fault tolerance support on the execution performance. For each application, its base code and a fault-tolerant version were executed on standard X10 and Resilient X10, and the computation times were compared. All of the measurements were done using four IBM® BladeCenter® HS23 (7875-C5J) blades, each of which consists of two 2.7-GHz Intel® Xeon® E5-2680 processors (a total of 16 cores). The machines were interconnected with 40-Gbps InfiniBand and running Red Hat Enterprise Linux® Server 6.3. The X10 was the Native X10 2.4.2 using the sockets communication layer, and Place 0 was used as the Resilient Storage. Each machine ran two places, so a total 8 places were used for the execution. Each application was compiled with “x10c++ -O4 -00 -no CHECKS”, and the time for executing the outermost for loop was measured. The print statements inside the loop were disabled. Each measurement was done 10 times and the best score was used.

Figure 8 shows the relative execution times normalized by the time of base code on standard X10 for each application. From left to right, each bar shows the score of the base code and its fault-tolerant version on standard X10, and their times on Resilient X10, respectively.

Comparing the execution times on standard X10, almost no overheads due to adding fault tolerance were
observed for MontePi and KMeans. For HeatTransfer, the fault-tolerant version took 9% more time, because of the cost of the periodic snapshots.

Next, the performance of each base code on standard and Resilient X10 was compared. In Resilient X10, the costs of at and async are larger since the critical states for the finish handling must be recorded in the Resilient Storage. Therefore, the execution becomes slightly slower, even for the base code. MontePi became about 2% slower because two at statements are executed for each place. KMeans became 8% slower since at is performed multiple times until the convergence. For HeatTransfer, the execution time increased by 6 times. This is mainly because at is invoked too frequently in the internal stencil computation.

By combining these overheads, compared to the case where the base code is executed on standard X10, running fault-tolerant code on Resilient X10 had 2.2% more overhead for MontePi and 9.0% more for KMeans. In contrast, HeatTransfer suffered a 6.5-fold slowdown. This can change with the snapshot frequency, and may be reduced by rewriting the application not to use unnecessary at calls.

5.3 Fault Tolerance
All of the results shown in the previous section are cases where no node failures occurred. Finally, we studied the behavior when nodes failed.

When an X10 process which corresponds to Place 2 was terminated externally by a kill command, the entire processing was aborted on standard X10 regardless of the fault tolerance of the application. Even in Resilient X10, base code applications were terminated by the DeadPlaceException (or enclosing Multiple-Exceptions). In contrast, when fault-tolerant versions were executed on Resilient X10, they could survive the place death and output the correct results. This means that the combination of fault-tolerant applications and Resilient X10 provided good fault tolerance. As a reference, an execution example of HeatTransfer with place deaths is shown in Figure 12 of appendix.

The effects caused by place deaths were also measured by running the fault-tolerant applications on Resilient X10. In MontePi, the deaths may reduce the accuracy of the results since the number of trials decreases. When 4 places among the 8 places were killed, the execution time did not increase, but the deviation of the calculated π value increased from 0.0008% to 0.002%. In KMeans and HeatTransfer, the place death increases both the number of iterations until convergence and the execution time of each iteration. When Place 2 was killed during the execution of the 17th iteration, execution time increased by 11% in KMeans and 14% in HeatTransfer, but the executions still ended with correct results.

6. Related Work
Usually, distributed processing is supported through libraries such as MPI [9], RMI [5], and the DB/Web access packages. In such cases, a node failure appears as a low-level error in the communication code. Therefore, fault tolerance must be supported by each application as error handling for the communication routines. In contrast, Resilient X10 can handle the node failure as part of its computation model [2, 3] by utilizing the characteristics of PGAS. Application modifications are still necessary to support fault tolerance, but we believe most cases are covered by the patterns presented in this paper. In addition, fault tolerance can be built into the application from the beginning, because the support exists inside the language.

How to handle node failures has been an important issue, especially in HPC applications that use massive numbers of computing nodes. The most popular approach is checkpointing [4] implemented by each application. Intermediate data is periodically saved, and when a failure occurs, the restarted application resumes the processing by restoring the data from the snapshot. The fault-tolerant HeatTransfer in Section 4.2 is based on the same idea, but most of the save and restore mechanisms are implemented in the general-purpose DistArray library, which makes the mechanisms easier to use. In addition, the application does not need to be restarted after node failures. In Hadoop [21], fault tolerance is achieved by writing the results of each phase to external storage (HDFS). This can be considered as a variation of the checkpointing approach.

Instead of restoring the data to get precise results, there is an interesting fault-tolerance approach of discarding only the failed results. The MontePi and KMeans in this paper can be considered as simple examples of this approach, but more detailed modeling to calculate probabilistic accuracy bounds has also been proposed [14]. We will take such models into account in developing larger fault-tolerant applications.

Recentlly, it has become common to perform large scale computations on virtualized (cloud) environments. In such situations, fault tolerance may be achieved by utilizing the snapshot [19] or migration [1, 8] functions for virtual machines [11]. However, this creates overhead to save or move entire virtual machines, so additional research is necessary to utilize them for distributed applications that use multiple computing nodes. One of the interesting topics is how Resilient X10 and its applications can benefit from virtualization.

7. Conclusions and Future Work
This paper described how fault-tolerant applications can be constructed using the “Resilient X10” exten-
Three methods of adding fault tolerance to existing applications are shown: (a) Ignore failures and use the results from the remaining nodes, (b) Reassign the failed node’s work to the remaining nodes, or (c) Restore the computation from a periodic snapshot. For all of these approaches, the code modifications were less than 25 lines. We also showed a distributed library, Resilient DistArray, which supports snapshot mechanisms.

Compared to the case where the original application is executed on standard X10, running fault-tolerant applications on Resilient X10 has 2.2% to 9.0% overhead if place change does not happen too frequently. We also noticed that there is a pathological case with a 6.5-fold slowdown if place changes are performed too frequently. The major cause of this overhead was the cost of periodic snapshots and the additional costs of at processing. However, by paying these costs, we confirmed that fault-tolerant applications can survive node failures. When one place among 8 places was lost, the execution time increased by 11–14%, although the exact number depends on the timing of the place death.

In the future, we want to reduce this overhead in fault-tolerant applications by improving both the applications and Resilient X10. Preparing more libraries that support fault tolerance is another topic. One candidate should be an interface to access the Resilient Storage from applications. We also plan to make fault-tolerant versions of larger distributed X10 applications, such as those described in [10] and [16].

Acknowledgments

We would like to thank the members of X10 project in IBM T. J. Watson Research Center and IBM Research - Tokyo, for their various suggestions and valuable comments. The Resilient X10 research was funded in part by the U. S. Air Force Office of Scientific Research under Contract No. FA8750-13-C-0052.

IBM and BladeCenter are trademarks of International Business Machines Corporation, registered in many jurisdictions worldwide. Other product and service names might be trademarks of IBM or other companies. A current list of IBM trademarks is available on the Web at “Copyright and trademark information” at www.ibm.com/legal/copytrade.shtml Java and all Java-based trademarks and logos are trademarks or registered trademarks of Oracle and/or its affiliates. Intel and Xeon are registered trademarks of Intel Corporation in the U.S. and/or other countries. Linux is a registered trademark of Linus Torvalds in the United States, other countries, or both.

References


import x10.regionarray.*;

class ResilientKMeans {
    static val DIM = 4n; // number of dimensions
    static val POINTS = 10000000; // number of points
    static val CLUSTERS = 4; // number of clusters to be categorized
    static val ITERATIONS = 1000; // number of maximum iterations

    public static def main(args:Rail[String]) {
        val place0 = here;
        // prepare a set of points (coordinates of i-th point are \((pt(1,0),pt(1,1),pt(1,2),pt(1,3))\)), which do not change after prepared
        val points_region = Region.make(0..(POINTS-1), 0..(DIM-1)), rnd = new x10.util.Random(0);
        val points_master = new Array[Float](points_region, (p:Point)=>rnd.nextFloat());
        val points_local = PlaceLocalHandle.make[Rail[Float]](PlaceGroup.WORLD, ()=>points_master); // deliver the point set to other places
        // an array to hold the cluster values (coordinates of k-th cluster are \([c1(k*4),c1(k*4+1),c1(k*4+2),c1(k*4+3)]\))
        val central_clusters = new Rail[Float](CLUSTERS*DIM, (i:Long)=>points_master(i/DIM, i%DIM)); // use i-th point as initial value
        // prepare data structures for the computation
        val old_central_clusters = new Rail[Float](CLUSTERS*DIM); // an array to hold the previous cluster values
        val central_cluster_counts = new Rail[Long](CLUSTERS); // number of points in each cluster
        val processed_points = new Cell[Long](0); // number of processed points
        // prepare global refs for remote access
        val central_cluster_counts_gr = GlobalRef(central_cluster_counts);
        val central_cluster_counts_gr = GlobalRef(central_cluster_counts);
        val processed_points_gr = GlobalRef(processed_points);
        // prepare three local arrays for processing at each place
        val localCurrClusters = PlaceLocalHandle.make[Rail[Float]](PlaceGroup.WORLD, ()=>new Rail[Float](CLUSTERS*DIM));
        val local_new_clusters = PlaceLocalHandle.make[Rail[Float]](PlaceGroup.WORLD, ()=>new Rail[Float](CLUSTERS*DIM));
        val local_cluster_counts = PlaceLocalHandle.make[Rail[Long]](PlaceGroup.WORLD, ()=>new Rail[Long](CLUSTERS));

        // prepareLocalHandle
        val local_cluster_counts = PlaceLocalHandle.make[Rail[Long]](PlaceGroup.WORLD, ()=>points_master);
        // number of maximum iterations
        val iterations = 1000;
        val old_central_clusters = new Rail[Float](CLUSTERS*DIM); // an array to hold the previous cluster values
        val central_cluster_counts = new Rail[Long](CLUSTERS); // number of points in each cluster
        val processed_points = new Cell[Long](0); // number of processed points
        // prepare global refs for remote access
        val central_cluster_counts_gr = GlobalRef(central_cluster_counts);
        val central_cluster_counts_gr = GlobalRef(central_cluster_counts);
        val processed_points_gr = GlobalRef(processed_points);
        // prepare three local arrays for processing at each place
        val localCurrClusters = PlaceLocalHandle.make[Rail[Float]](PlaceGroup.WORLD, ()=>new Rail[Float](CLUSTERS*DIM));
        val local_new_clusters = PlaceLocalHandle.make[Rail[Float]](PlaceGroup.WORLD, ()=>new Rail[Float](CLUSTERS*DIM));
        val local_cluster_counts = PlaceLocalHandle.make[Rail[Long]](PlaceGroup.WORLD, ()=>new Rail[Long](CLUSTERS));

        // prepareLocalHandle
        val local_cluster_counts = PlaceLocalHandle.make[Rail[Long]](PlaceGroup.WORLD, ()=>points_master);
        // number of maximum iterations
        val iterations = 1000;
        val old_central_clusters = new Rail[Float](CLUSTERS*DIM); // an array to hold the previous cluster values
        val central_cluster_counts = new Rail[Long](CLUSTERS); // number of points in each cluster
        val processed_points = new Cell[Long](0); // number of processed points
        // prepare global refs for remote access
        val central_cluster_counts_gr = GlobalRef(central_cluster_counts);
        val central_cluster_counts_gr = GlobalRef(central_cluster_counts);
        val processed_points_gr = GlobalRef(processed_points);
        // prepare three local arrays for processing at each place
        val localCurrClusters = PlaceLocalHandle.make[Rail[Float]](PlaceGroup.WORLD, ()=>new Rail[Float](CLUSTERS*DIM));
        val local_new_clusters = PlaceLocalHandle.make[Rail[Float]](PlaceGroup.WORLD, ()=>new Rail[Float](CLUSTERS*DIM));
        val local_cluster_counts = PlaceLocalHandle.make[Rail[Long]](PlaceGroup.WORLD, ()=>new Rail[Long](CLUSTERS));

        // prepareLocalHandle
        val local_cluster_counts = PlaceLocalHandle.make[Rail[Long]](PlaceGroup.WORLD, ()=>points_master);
        // number of maximum iterations
        val iterations = 1000;
        val old_central_clusters = new Rail[Float](CLUSTERS*DIM); // an array to hold the previous cluster values
        val central_cluster_counts = new Rail[Long](CLUSTERS); // number of points in each cluster
        val processed_points = new Cell[Long](0); // number of processed points
        // prepare global refs for remote access
        val central_cluster_counts_gr = GlobalRef(central_cluster_counts);
        val central_cluster_counts_gr = GlobalRef(central_cluster_counts);
        val processed_points_gr = GlobalRef(processed_points);
        // prepare three local arrays for processing at each place
        val localCurrClusters = PlaceLocalHandle.make[Rail[Float]](PlaceGroup.WORLD, ()=>new Rail[Float](CLUSTERS*DIM));
        val local_new_clusters = PlaceLocalHandle.make[Rail[Float]](PlaceGroup.WORLD, ()=>new Rail[Float](CLUSTERS*DIM));
        val local_cluster_counts = PlaceLocalHandle.make[Rail[Long]](PlaceGroup.WORLD, ()=>new Rail[Long](CLUSTERS));

        // prepareLocalHandle
    }
}

A. Appendix

A.1 Full Code of Fault-Tolerant KMeans and HeatTransfer

The complete code of KMeans and HeatTransfer is shown in Figures 9, 10, and 11. These programs can be compiled and executed by the latest X10 distribution, 2.4.2. Similar programs are also included in the distribution, including MontePi and multiple Resilient DistArray implementations, under the directory samples/resiliency/. Refer to the README.txt file in the directory for details.

A.2 Example of Fault-Tolerant Execution

Figure 12 shows the behavior of the fault-tolerant HeatTransfer included in the samples. The program was compiled by Native X10 and executed for 10x10 size using 8 places. A new snapshot was created at every 10th iteration (shown in Line 42, etc.).

When the DistArray is (re)constructed, this program reports how the 2-dimensional grid points are mapped to the places. During the execution, Places 2 and 7 were terminated by kill11 commands, and the output shows that that DPEs were appropriately notified and the DistArray was correctly reconstructed over the remaining live places (Lines 74 and 101).
for (iter in 1..ITERATIONS) { Console.OUT.println("Iteration " + iter); // iterate until the result converges
    // 1. deliver current cluster values to other places
    try {
        finish for (pl in Place.places()) { if (pl.isDead()) continue; // skip dead place(s)
            at (pl) async { // compute at live places in parallel
                for (var j:Long = 0; j < CLUSTERS*DIM; ++j) {
                    local_curr_clusters()(j) = central_clusters(j); local_new_clusters()(j) = 0f;
                }
            }
            } }
        catch (es:MultipleExceptions) { // just ignore place death
            for (e in es.exceptions()) if ( !(e instanceof DeadPlaceException)) throw e; }
        }
    // 2. save current cluster values and clear them
    for (var j:Long = 0; j < CLUSTERS*DIM; ++j) { old_central_clusters(j) = central_clusters(j); central_clusters(j) = 0f; }
    for (var j:Long = 0; j < CLUSTERS; ++j) central_cluster_counts(j) = 0;
    // 3. process some part of the points at each place
    val numAvail = Place.MAX_PLACES - Place.numDead(); // number of live places
    val div = POINTS / numAvail, rem = POINTS % numAvail; // share for each place, and extra share for Place 0
    var start:Long = 0; // next point to be processed
    try {
        finish for (pl in Place.places()) { if (pl.isDead()) continue; // skip dead place(s)
            var end:long = start + div; if (pl=place0) end += rem; // points [start,end) are processed in this place
                val s = start, e = end;
            at (pl) async { // compute at live places in parallel
                for (var p = 0; p < s; ++p) { val f = p; // process the p-th point
                    val points = points_local(); var closest:long = -1, closest_dist:Float = Float.MAX_VALUE;
                        for (var k:long = 0; k < CLUSTERS; ++k) { // find the closest cluster
                            var dist:Float = Float.MAX_VALUE;
                                for (var d:long = 0; d < DIM; ++d) { // calculate the distance to the k-th cluster
                                    val tmp = points(p,d) - local_curr_clusters()(k*DIM+d);
                                        dist = tmp * tmp;
                                    }
                                        if (dist < closest_dist) { closest = k; }
                                    }
                                }
                                local_cluster_coords(closest)(); // add the coordinates of the point to the closest cluster
                            }
                        }
                    }
                    } // end of the processing of assigned points
                val tmp = local_new_clusters(computed_cluster_counts)() += points(p,d);
            } }
        catch (es:MultipleExceptions) { // just ignore place death
            for (e in es.exceptions()) if ( !(e instanceof DeadPlaceException)) throw e; }
        }
    // 4. compute new cluster values, and check the convergence
    for (var j:Long = 0; j < CLUSTERS; ++j) { central_clusters_gr()() += central_cluster_counts(j);
        if (processed_points() == POINTS) { // perform the convergence check only when all points are processed
            b:Boolean = true;
            for (var j:Long = 0; j < CLUSTERS*DIM; ++j) { // just CLUSTERS*DIM: ++j)
                if (Math.abs(old_central_clusters(j) - central_clusters(j)) > 0.0001) { b = false; break; }
            }
            if (b) break; // exit the iteration if converged
        }
    }
    start = end;
    // end of finish, wait for the execution in all places
    } catch (es:MultipleExceptions) { // just ignore place death
        for (e in es.exceptions()) if ( !(e instanceof DeadPlaceException)) throw e; }
    // print the result in the central_clusters array
    for (var d:Long = 0; d < DIM; ++d) { Console.OUT.println("%10.8f ", central_clusters(k*DIM+d));
        Console.OUT.println("--- dim " + d);
    }
}

Figure 10. Fault-tolerant KMeans.
import x10.regionarray.*;

class ResilientHeatTransfer {
    static val N = 28; // size of grid
    static val ITERATIONS = 1000; // number of maximum iterations
    static val livePlaces = new x10.util.ArrayList[Place](); // set of live places
    static val restore_needed = new Cell[Boolean](false); // flag to indicate restoration is necessary

    public static def main(args:Rail[String]) {
        for (pl in Place.places()) livePlaces.add(pl);
        val BigR = Region.make(0..(N+1), 0..(N+1)); // 2-dimensional region which includes surroundings
        val SmallR = Region.make(1..N, 1..N); // 2-dimensional N x N region, which does not include surroundings
        val LastRow = Region.make(0..N, 0..1); // heated area at the top
        // create data which will be recreated at place death
        var BigD:Dist(2) = Dist.makeBlock(BigR, 0, new SparsePlaceGroup(livePlaces.toRail()));
        var SmallD:Dist(2) = BigD|SmallR;
        var D_Base:Dist = Dist.makeUnique(SmallD.places());
        // create distributed arrays (each element holds a heat value and the LastRow area is always 1.0)
        val A = ResilientDistArray.make[Double](BigD, (p:Point)=>{ LastRow.contains(p) ? 1.0 : 0.0 });
        val Temp = ResilientDistArray.make[Double](BigD); // a DistArray to hold newly calculated values temporarily
        val Scratch = ResilientDistArray.make[Double](BigD);
        A.snapshot(); // create the initial snapshot
        for (iter in 1..ITERATIONS) { Console.OUT.println("Iteration " + iter); // iterate until the result converges
            try {
                // 1. if necessary, restore data from the snapshot
                if (restore_needed) {
                    // recreate Dist over the remaining live places
                    BigD = Dist.makeBlock(BigR, 0, new SparsePlaceGroup(livePlaces.toRail()));
                    SmallD = BigD|SmallR;
                    D_Base = Dist.makeUnique(SmallD.places());
                    A.restore(BigD); // reconstruct DistArray with the new Dist, and restore elements from the snapshot
                    Temp remake(BigD); Scratch remake(BigD);
                    restore_needed = false;
                }
                // 2. core part of the heat transfer computation
                val D = SmallD;
                finish atexch (2 in D_Base) { // distributed processing at each place
                    for (p:Point in D here) { // process the points of this place
                        val [x,y] = p; // stencil computation, average of surrounding four points becomes the new heat value
                        Temp(p) = ( (at (A.dist(x-1,y)) A(x-1,y)) + (at (A.dist(x,y+1)) A(x,y+1))
                                + (at (A.dist(x,y-1)) A(x,y-1)) + (at (A.dist(x,y+1)) A(x,y+1)) ) / 4; //
                    }
                }
                // 3. check the convergence
                val delta = A.map(Temp, D.region, (a:Double,b:Double)=>Math.abs(a-b))
                        .reduce((a,Double,b:Double)=>Math.max(a,b), 0.0);
                Temp.map(A, Temp, D.region, (a:Double,b:Double)=>a); // copy the new results in Temp to A in parallel
                if (delta <= 0.0001) break; // exit the iteration if converged
                // 4. create a snapshot at every 10th iteration
                if (iter % 10 == 0) A.snapshot();
                catch (e:Exception) { processException(e); } // process an exception
                } end of for (iter)
            }
        // print the result in the distributed array A
        for ([x] in A.region.projection(0)) {
            for ([y] in A.region.projection(1)) Console.OUT.println("5.3f ", at (A.dist(x,y)) A(x,y));
            Console.OUT.println();
        }
    }
}

Figure 11. Fault-tolerant HeatTransfer.
Figure 12. Behavior of HeatTransfer with node failures.